

8.1.xa. Exercise answers

1. a. *Someone is missing*

($\exists x$: x is a person) x is missing

$$\begin{aligned} & (\exists x: Px) Mx \\ & \exists x (Px \wedge Mx) \end{aligned}$$

[M: λx (x is missing); P: λx (x is a person)]

- b. *No one found the loot.*

\neg *someone found the loot*

\neg *someone is such that (he or she found the loot)*

\neg ($\exists x$: \underline{x} is a person) \underline{x} found the loot

$$\begin{aligned} & \neg (\exists x: Px) Fxl \\ & \neg \exists x (Px \wedge Fxl) \end{aligned}$$

[F: λxy (x found y); P: λx (x is a person); l: the loot]

- c. *There is a tavern in the town*

Something is a tavern in the town

Something is such that (it is a tavern in the town)

$\exists x$ x is a tavern in the town

$\exists x$ (\underline{x} is a tavern \wedge \underline{x} is in the town)

$$\exists x (Tx \wedge Ixt)$$

[I: λxy (x is in y); T: λx (x is a tavern); t: the town]

It would also be possible to understand *in the town* to modify the verb *is* rather than the noun *tavern*. In that case, the sentence could be restated as *A tavern is in the town* and be analyzed using a restricted existential.

- d. *Some winner of the lottery has not come forward*

Some winner of the lottery is such that (he or she has not come forward)

($\exists x$: x is a winner of the lottery) x has not come forward

($\exists x$: \underline{x} is a winner of the lottery) \neg \underline{x} has come forward

$$\begin{aligned} & (\exists x: Wxl) \neg Fx \\ & \exists x (Wxl \wedge \neg Fx) \end{aligned}$$

[F: λx (x has come forward); W: λxy (x is a winner of y); l: the lottery]

- e. *Tod watched a dance troop from India*

A dance troop from India is such that (Tod watched it)

$(\exists x: x \text{ is a dance troop from India}) \underline{\text{Tod}} \text{ watched } \underline{x}$
 $(\exists x: \underline{x} \text{ is a dance troop} \wedge \underline{x} \text{ is from } \underline{\text{India}}) \text{ Wtx}$

$(\exists x: Dx \wedge Fxi) \text{ Wtx}$
 $\exists x ((Dx \wedge Fxi) \wedge \text{Wtx})$

[D: $\lambda x (x \text{ is a dance troop})$; F: $\lambda xy (x \text{ is from } y)$; W: $\lambda xy (x \text{ watched } y)$; i: *India*; t: *Tod*]

- f. *The search turned up no car fitting the description*
 \neg *the search turned up a car fitting the description*
 \neg *a car fitting the description is such that (the search turned it up)*
 $\neg (\exists x: x \text{ is a car fitting the description}) \underline{\text{the search}} \text{ turned up } \underline{x}$
 $\neg (\exists x: \underline{x} \text{ is a car} \wedge \underline{x} \text{ fit } \underline{\text{the description}}) \text{ Tsx}$

$\neg (\exists x: Cx \wedge Fxd) \text{ Tsx}$
 $\neg \exists x ((Cx \wedge Fxd) \wedge \text{Tsx})$

[C: $\lambda x (x \text{ is a car})$; F: $\lambda xy (x \text{ fit } y)$; T: $\lambda xy (x \text{ turned up } y)$; d: *the description*; s: *the search*]

- g. *There is a button behind you that will open the door*
Something is a button behind you that will open the door
Something is such that (it is a button behind you that will open the door)

$\exists x x \text{ is a button behind you that will open the door}$
 $\exists x (x \text{ is a button behind you} \wedge \underline{x} \text{ will open } \underline{\text{the door}})$
 $\exists x ((\underline{x} \text{ is a button} \wedge \underline{x} \text{ is behind } \underline{\text{you}}) \wedge \text{Oxd})$

$\exists x ((Bx \wedge Hxo) \wedge \text{Oxd})$

[B: $\lambda x (x \text{ is a button})$; H: $\lambda xy (x \text{ is behind } y)$; O: $\lambda xy (x \text{ will open } y)$; d: *the door*; o: *you*]

If the prepositional phrase *behind you* is understood to modify *is* instead of *button*, the sentence could be restated as *A button that will open the door is behind you*. This sentence would be analyzed by the restricted existential $(\exists x: Bx \wedge \text{Oxd}) Hxo$, in which two of the conjuncts from the quantified predicate in the analysis above appear instead in the restriction of the quantifier.

- h. *If Tom doesn't find anything, he'll be disappointed*
Tom won't find anything → *Tom will be disappointed*
 ¬ *Tom will find something* → Tom *will be disappointed*
 ¬ *something is such that (Tom will find it)* → Dt
 ¬ ∃x Tom *will find* x → Dt
 ¬ ∃x Ftx → Dt

[D: λx (x will be disappointed); F: λxy (x will find y); t: Tom]

- i. *Al went to a restaurant no one he knew had heard of*
A restaurant no one Al knew had heard of is such that
(Al went to it)

($\exists x$: x is a restaurant no one Al knew had heard of) Al
 went to x

($\exists x$: x is a restaurant \wedge no one Al knew had heard of x)
 Wax

($\exists x$: Rx \wedge ¬ someone Al knew had heard of x) Wax

($\exists x$: Rx \wedge ¬ someone Al knew is such that (he or she had
 heard of x)) Wax

($\exists x$: Rx \wedge ¬ ($\exists y$: y is a person Al knew) y had heard of x)
 Wax

($\exists x$: Rx \wedge ¬ ($\exists y$: y is a person \wedge Al knew y) Hyx) Wax

($\exists x$: Rx \wedge ¬ ($\exists y$: Py \wedge Kay) Hyx) Wax

$\exists x ((Rx \wedge \neg \exists y ((Py \wedge Kay) \wedge Hyx)) \wedge Wax)$

H: λxy (x had heard of y); K: λxy (x knew y); P: λx (x is a
 person); R: λx (x is a restaurant); W: λxy (x went to y); a:
 Al]

2. a. $\exists x$ x is burning
 something is such that (it is burning)

Something is burning

or: *There is something burning*

- b. ($\exists x$: x is a person) x is at the door
 someone is such that (he or she is at the door)

Someone is at the door

- c. ($\exists x$: x is a fire) Tamara reported x
 Some fire is such that (Tamara reported it)

Tamara reported a fire

- d. $\neg (\exists x: x \text{ is a person} \wedge x \text{ was in the room})$ x knew Sam
 $\neg (\exists x: x \text{ was a person in the room})$ x knew Sam
 \neg someone in the room is such that (he or she knew Sam)
 \neg someone in the room knew Sam

No one in the room knew Sam

- e. $(\exists x: x \text{ is a vase})$ (Vic touched x \wedge x shattered)
 $(\exists x: x \text{ is a vase})$ (Vic touched x and x shattered)
 A vase is such that (Vic touched it and it shattered)

Vic touched a vase and it shattered

- f. $\exists x (x \text{ had happened} \wedge \text{Jane left to deal with } x)$
 $\exists x$ x had happened and Jane left to deal with x
 something is such that (it had happened and Jane left to deal with it)

Something had happened and Jane left to deal with it

- g. $\exists x (\text{Ann forgot } x \wedge \text{Bill remembered } x)$
 $\exists x (\text{Ann forgot } x \text{ and Bill remembered } x)$
 something is such that (Ann forgot it and Bill remembered it)

Ann forgot something and Bill remembered it
 or: *There is something that Ann forgot and Bill remembered*

- h. $(\exists x: x \text{ was fast} \wedge x \text{ was heavy})$ the instrument detected x
 $(\exists x: x \text{ was fast and heavy})$ the instrument detected x
 $(\exists x: x \text{ is a thing that was fast and heavy})$ the instrument detected x

Something that was fast and heavy was such that (the instrument detected it)

The instrument detected something that was fast and heavy

or: *The instrument detected something fast and heavy*