## 6.1.xa. Exercise answers

1. a. <u>Ann</u> introduced <u>Bill</u> to <u>Carol</u>
[λxyz (x introduced y to z)] Ann Bill Carol

Iabc I fits a, b, 'n c

[I: λxyz (x introduced y to z); a: Ann; b: Bill; c: Carol]

Ann gave the book to either Bill or Carol
Ann gave the book to Bill v Ann gave the book to Carol
[λxyz (x gave y to z)] Ann the book Bill v [λxyz (x gave y to z)]
Ann the book Carol

Gakb v Gakc either G fits a, k, 'n b or G fits a, k, 'n c

[G: λxyz (x gave y to z); a: Ann; b: Bill; c: Carol; k: the book]

C. Ann gave the book to Bill and he gave it to Carol Ann gave the book to Bill ∧ Bill gave the book to Carol [λxyz (x gave y to z)] Ann the book Bill ∧ [λxyz (x gave y to z)] Bill the book Carol

 $Gakb \wedge Gbkc \\ \mbox{both $G$ fits $a, k, 'n $b$ and $G$ fits $b, k, 'n $c$} \\$ 

[G: λxyz (x gave y to z); a: Ann; b: Bill; c: Carol; k: the book]
d. Tom had the package sent to Sue, but it was returned to him Tom had the package sent to Sue ∧ the package was returned to Tom

 $[\lambda xyz (x had y sent to z)] \underline{Tom} \underline{the package} \underline{Sue} \wedge [\lambda xy (x was returned to y)] \underline{the package} \underline{Tom}$ 

 $Htps \wedge Rpt \\ both \; H \; \text{fits} \; t, \; p, \; 'n \; s \; \text{and} \; R \; \text{fits} \; p \; 'n \; t \\$ 

[H:  $\lambda xyz$  (x had y sent to z); R:  $\lambda xy$  (x was returned to y); p: the package; s: Sue; t: Tom]

**e.** Georgia will see Ed if she gets to Denver before Saturday Georgia will see Ed ← Georgia will get to Denver before Saturday

[ $\lambda xy (x will see y)$ ] <u>Georgia Ed</u>  $\leftarrow$  [ $\lambda xyz (x will get to y before z)] <u>Georgia Denver Saturday</u>$ 

 $Sge \leftarrow Ggds$   $Ggds \rightarrow Sge$ 

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if G fits g, d, 'n s then S fits g 'n e
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[G: λxyz (x will get to y before z); S: λxy (x will see y); d: Denver; e: Ed; g: Georgia; s: Saturday]

**f.** If the murderer is either the butler or the nephew, then I'm Sherlock Holmes

the murderer is either the butler or the nephew  $\rightarrow$  <u>I</u>'m <u>Sherlock</u> Holmes

(<u>the murderer</u> is <u>the butler</u>  $\vee$  <u>the murderer</u> is <u>the nephew</u>)  $\rightarrow$  <u>I</u> = Sherlock Holmes

 $(\underline{the\ murderer} = \underline{the\ butler} \lor \underline{the\ murderer} = \underline{the\ nephew}) \rightarrow i$ = s

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(m = b \lor m = n) \rightarrow i = s
if either m is b or m is n then i is s
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[b: the butler; i: I; m: the murderer; n: the nephew; s: Sherlock Holmes]

- g. Neither Ann nor Bill saw Tom speak to either Mike or Nancy
  - ¬ (Ann saw Tom speak to either Mike or Nancy ∨ Bill saw Tom speak to either Mike or Nancy)
  - ¬ ((<u>Ann</u> saw <u>Tom</u> speak to <u>Mike</u> v <u>Ann</u> saw <u>Tom</u> speak to <u>Nancy</u>) v (<u>Bill</u> saw <u>Tom</u> speak to <u>Mike</u> v <u>Bill</u> saw <u>Tom</u> speak to Nancy))
  - ¬ (([λxyz (x saw y speak to z)] <u>Ann Tom Mike</u> v [λxyz (x saw y speak to z)] <u>Ann Tom Nancy</u>) v ([λxyz (x saw y speak to z)] Bill Tom Mike v [λxyz (x saw y speak to z)] Bill Tom Nancy))

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¬ ((Satm v Satn) v (Sbtm v Sbtn))
not either either S fits a, t, 'n m or S fits a,t, 'n n
or either S fits b,t, 'n m or S fits b,t, 'n n
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[S: λxyz (x saw y speak to z); a: Ann; b: Bill; m: Mike; n: Nancy; t: Tom]

**h.** Tom will agree if each of Ann, Bill, and Carol asks him Tom will agree  $\leftarrow$  each of Ann, Bill, and Carol will ask Tom  $\underline{Tom}$  will agree  $\leftarrow$  ((Ann will ask  $\underline{Tom} \land \underline{Bill}$  will ask  $\underline{Tom}$ )  $\land$   $\underline{Carol}$  will ask  $\underline{Tom}$ )

 $[\lambda x (x will agree)] \underline{Tom} \leftarrow (([\lambda xy (x will ask y)] \underline{Ann} \underline{Tom} \land [\lambda xy (x will ask y)] \underline{Bill} \underline{Tom}) \land [\lambda xy (x will ask y)] \underline{Carol} \underline{Tom})$ 

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Gt \leftarrow ((Aat \land Abt) \land Act)
((Aat \land Abt) \land Act) \rightarrow Gt
if both both A fits a 'n t and A fits b 'n t and A
fits c 'n t then G fits t
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[A:  $\lambda xy$  (x will ask y); G:  $\lambda x$  (x will agree); a: Ann; b: Bill; c: Carol; t: Tom]

The function of *each* here is to indicate a group of two-place predication rather than a single four-place predicate  $\lambda xyzw$  (x, y, *and* z *will ask* w), which is what would be required in order to express instead the idea of Ann, Bill, and Carol making the request as a group.

Crawfordsville is west of Indianapolis and south of Lafayette

**b.**  $[\lambda xy (x \text{ has met y})] \underline{Ann Bill} \rightarrow [\lambda xy (x \text{ has met y})] \underline{Bill Ann}$ Ann has met Bill  $\rightarrow Bill \text{ has met Ann}$ If Ann has met Pill then he has met hen

If Ann has met Bill then he has met her

c. [λxyz (x introduced y to z)] <u>Alice Clarice Boris</u>

 Λ [λxyz (x introduced y to z)] <u>Alice Doris Boris</u>

 Alice introduced Clarice to Boris Λ Alice introduced Doris to Boris

Alice introduced Clarice and Doris to Boris

**d.** [λxy (x wrote to y)] Alice Boris

 $\land$  [ $\land$ xyzw (x asked y to write z about w)] <u>Alice Boris Alice</u> Boris

Alice wrote to Boris Alice asked Boris to write Alice about Boris

Alice wrote to Boris \( \lambda \) Alice asked Boris to write her about himself

Alice wrote to Boris and asked him to write her about himself

**e.**  $g = c \rightarrow (f = s \land p = t)$ 

 $\frac{Green\ Bay}{the\ team} = \underline{the\ city} \rightarrow (\underline{football} = \underline{the\ sport} \land \underline{the\ Packers} = \underline{the\ team})$ 

Green Bay is the city → (football is the sport  $\land$  the Packers are the team)

Green Bay is the city  $\rightarrow$  football is the sport and the Packers are the team

If Green Bay is the city, then football is the sport and the Packers are the team

Glen Helman 15 Oct 2004