## 2.3.x. Exercise questions

Use the basic system of derivations to check each of the claims below; if a derivation indicates that a claim fails, present a counterexample (that is, give an interpretation that divides an open gap and calculate truth values for the premises and conclusion from it—as is done in the example in 2.3.3):

- 1.  $A \Rightarrow A \wedge B$
- **2.**  $A \wedge B \Rightarrow A \wedge (B \wedge A)$
- 3.  $B \wedge E, C \wedge \top \Rightarrow (A \wedge B) \wedge (C \wedge D)$
- **4.** A  $\wedge$  B, B  $\wedge$  C, C  $\wedge$  D  $\Rightarrow$  A  $\wedge$  D
- 5. A, B  $\wedge$  A, D  $\Rightarrow$  B  $\wedge$  ((C  $\wedge$  A)  $\wedge$  D)

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